



Simulations of IBS for HL-LHC Protons



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Thanks to John Jowett, Roderik Bruce

Outline

- ▶ Collider Time Evolution (CTE) program – IBS simulations
- ▶ Current LHC simulations done with CTE
 - ▶ published in [CERN-ATS-Note-2012-044 PERF](#)
- ▶ HL-LHC calculations with MADX based on ATS optics

- ▶ Benchmark Case Proposal
- ▶ Future Plans

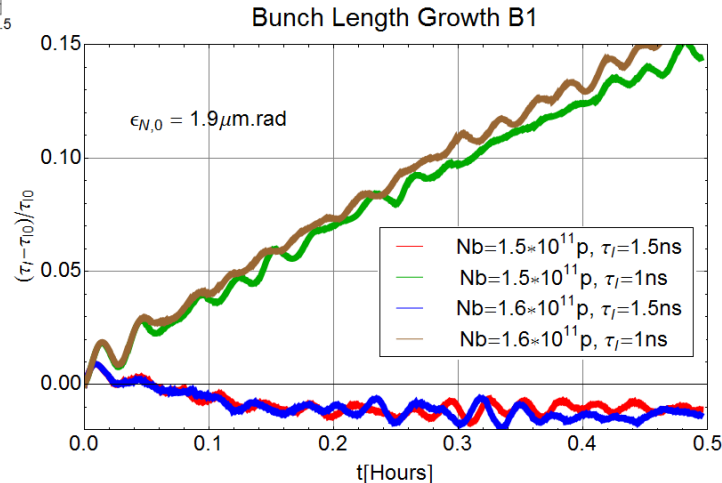
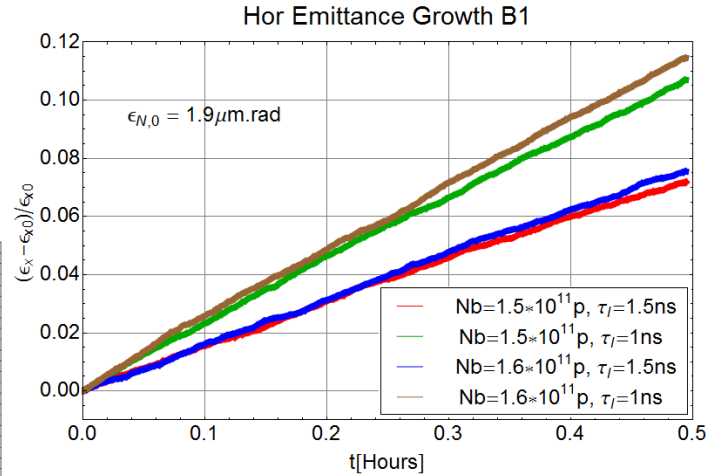
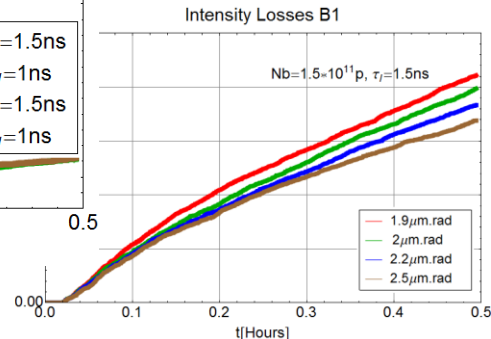
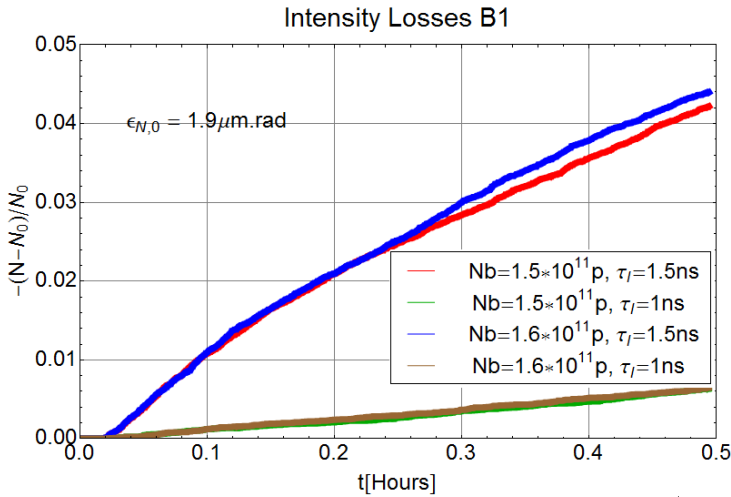
Collider Time Evolution (CTE) Program

- ▶ Authors: Mike Blaskiewicz, Roderik Bruce and Tom Mertens
- ▶ Program to track 2 bunches of **macro-particles** in time in a collider
 - ▶ Subroutines act on the bunches on a **turn-by-turn basis**: one simulation turn can correspond to any chosen number of machine turns.
 - ▶ Several other input parameter define the initial beams: e.g. particle type, particles per bunch, emittances in X and Y, bunch length, RF voltage...
 - ▶ IBS effects are simulated but no Beam-Beam

LHC in 2012



LHC Protons in 2012 - Injection

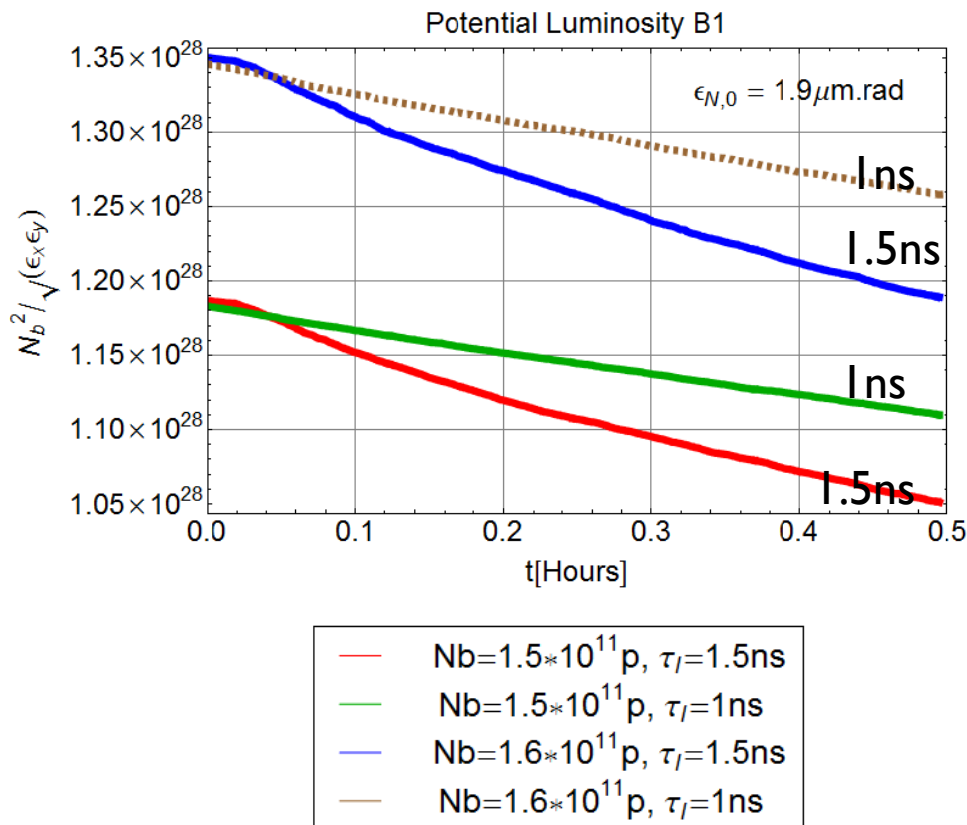


loss mechanisms

- ▶ particles leave bucket (debunching losses)
- ▶ hit physical aperture (due to dispersion or betatron action)
- ▶ highest losses but smaller transverse and longitudinal emittance blow up for bunches with great initial bunch length (1.5ns)
- ▶ blow up and losses increase with smaller initial emittances
- ▶ no big difference for different initial intensities

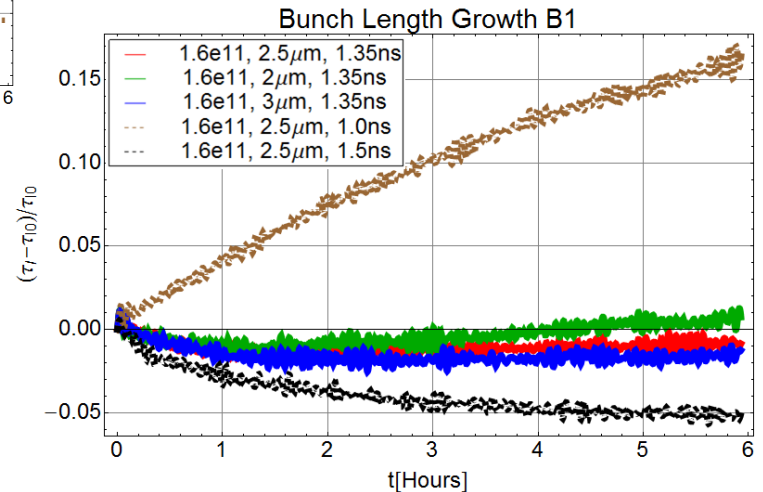
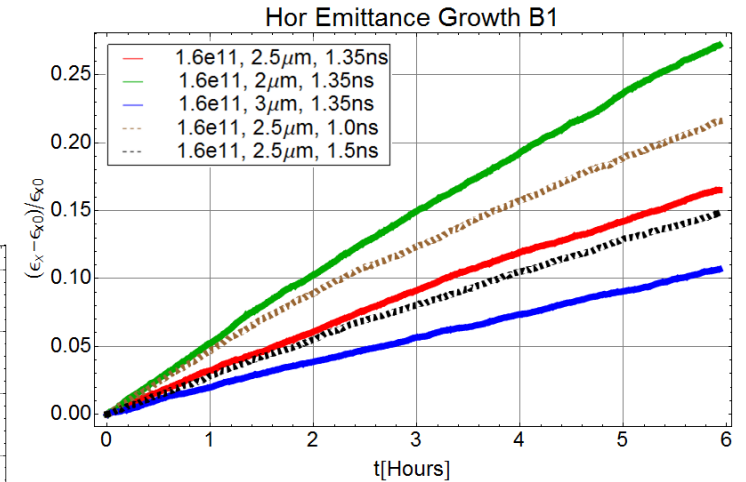
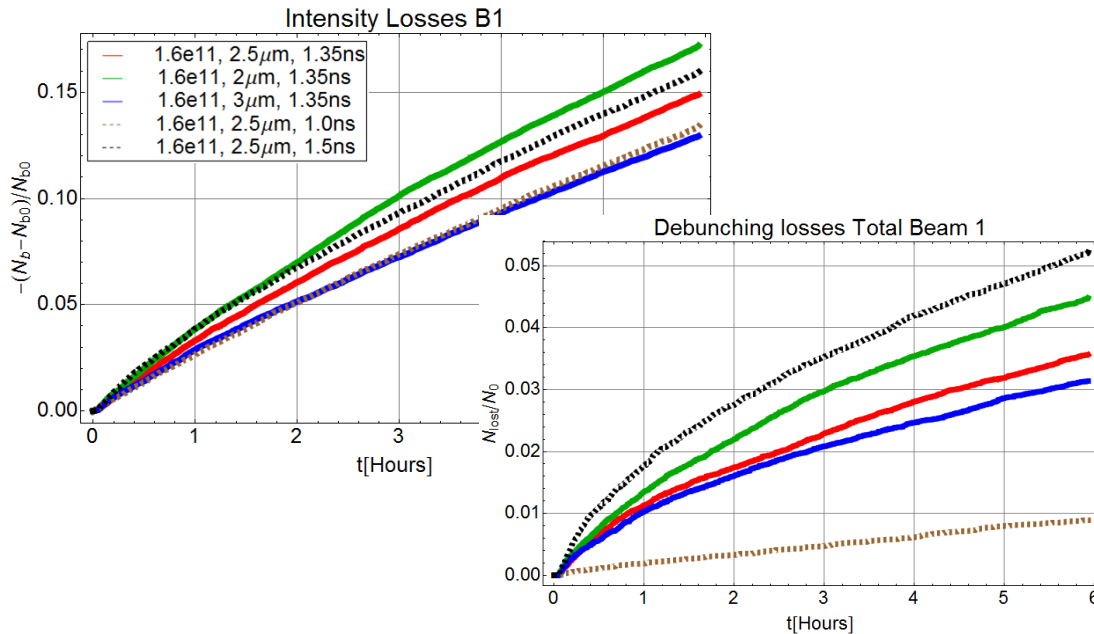
LHC Protons in 2012 – Effect of injection conditions on Luminosity

Figure of merit for initial luminosity vs. time spent at injection



- ▶ calculate $N^2 / \sqrt{\epsilon_x \epsilon_y}$ to get an estimate of what the luminosity would be if collisions were started
- ▶ curves for the 1ns initial bunch length cases decrease slower
 - ▶ less intensity losses, since the particles fill the bucket before they start to get lost
- ▶ the high particle losses of the blown-up bunches decrease the expected luminosity much more, even if their emittance blow-up is slower
- ▶ a compromise for the blow-up of the longitudinal emittance has to be found, to optimize the initial luminosity (and luminosity lifetime later)

LHC Protons in 2012 – Physics @ 4TeV

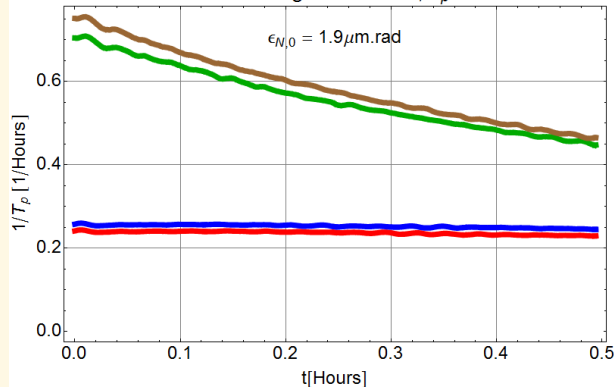


- ▶ total intensity losses are the sum of debunching and luminosity losses
 - ▶ significant differences in debunching losses: they become more important for greater bunch lengths
 - ▶ total losses dominated by luminosity burn-off
- ▶ smaller initial transverse emittances lose more and grow faster
- ▶ small initial bunch length grow faster

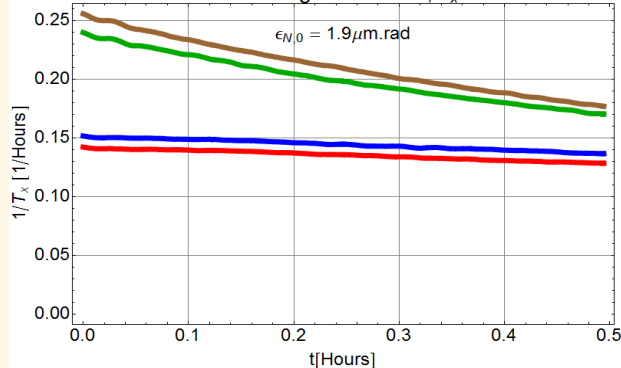
LHC Protons in 2012 – IBS Growth Rates

Injection

B1 IBS growth rate $1/T_p$



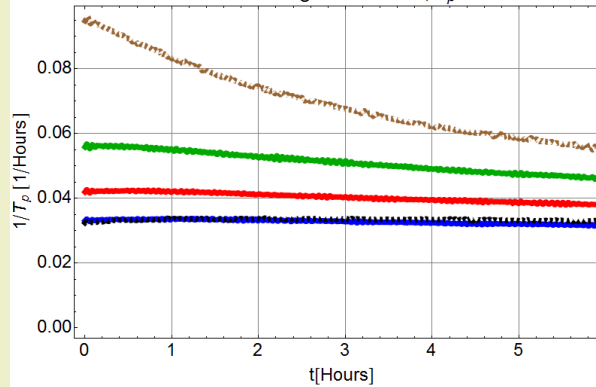
B1 IBS growth rate $1/T_x$



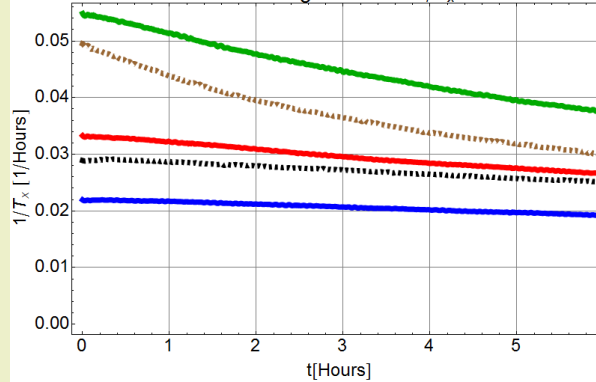
- $N_b=1.5 \times 10^{11} p, \sigma_t=1.5 ns$
- $N_b=1.5 \times 10^{11} p, \sigma_t=1 ns$
- $N_b=1.6 \times 10^{11} p, \sigma_t=1.5 ns$
- $N_b=1.6 \times 10^{11} p, \sigma_t=1 ns$

Collisions@4TeV

B1 IBS growth rate $1/T_p$



B1 IBS growth rate $1/T_x$



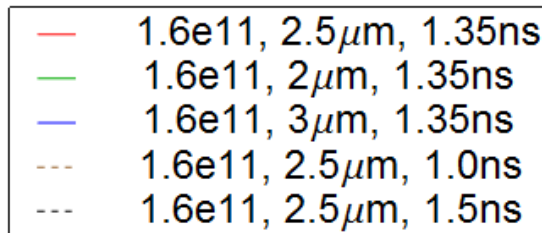
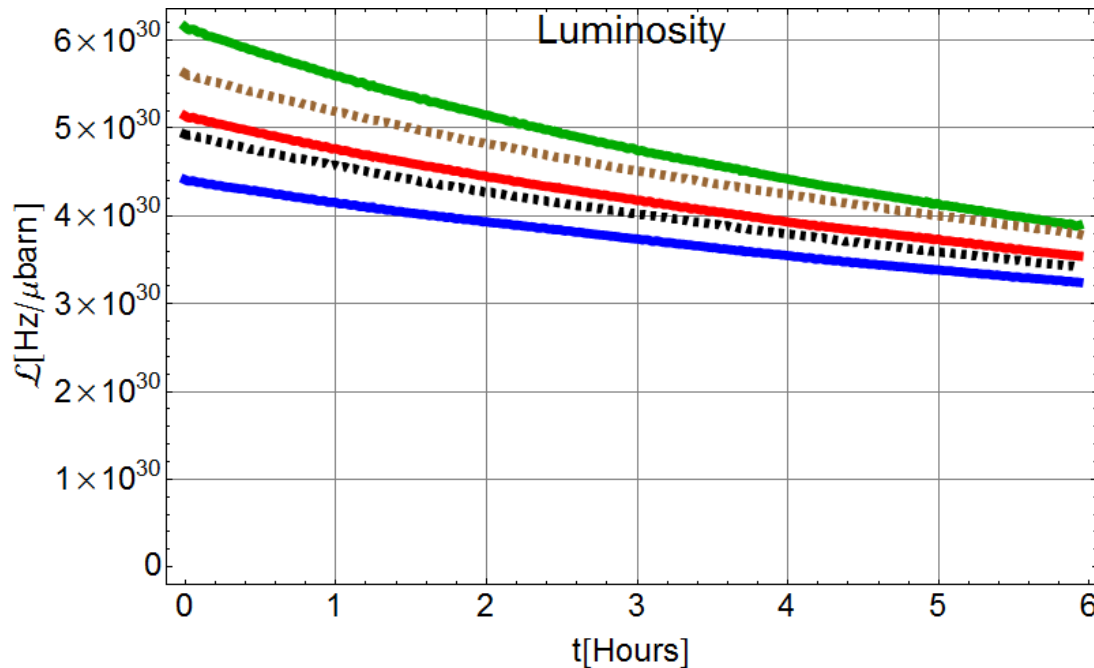
- $1.6e11, 2.5 \mu m, 1.35 ns$
- $1.6e11, 2 \mu m, 1.35 ns$
- $1.6e11, 3 \mu m, 1.35 ns$
- $1.6e11, 2.5 \mu m, 1.0 ns$
- $1.6e11, 2.5 \mu m, 1.5 ns$

- ▶ small initial bunch length leads to higher IBS growth rates which decrease fast
- ▶ growth rates for higher initial length are quite stable and much smaller
- ▶ initial growth rate increases with smaller initial emittance

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LHC Protons in 2012 - Luminosity



- ▶ bunch with smallest emittance has highest luminosity
- ▶ bunches with different initial bunch lengths show different initial luminosities
 - ▶ effect in agreement with the geometric luminosity reduction due to the crossing angle

$$F = 1 / \sqrt{1 + \left(\frac{\theta_c \sigma_z}{2\sigma_{xy}}\right)^2}$$

- ▶ 1.5ns case smallest luminosity – has highest debunching losses

HL-LHC

HL-LHC Beam Parameters

Beam parameters from HL-LHC Kick off:	25 ns	25ns (short)	50 ns
# protons / bunch [1E11]	2.2	2.2	3.5
Longitudinal emittance [eV.s]	2.5	~1.4	2.5
Rms bunch length [cm]	7.5	4	7.5
Rms momentum spread [1E-4]	1	~1	1
Normalized rms transverse emittance [microm]	2.5	3.0	3.0

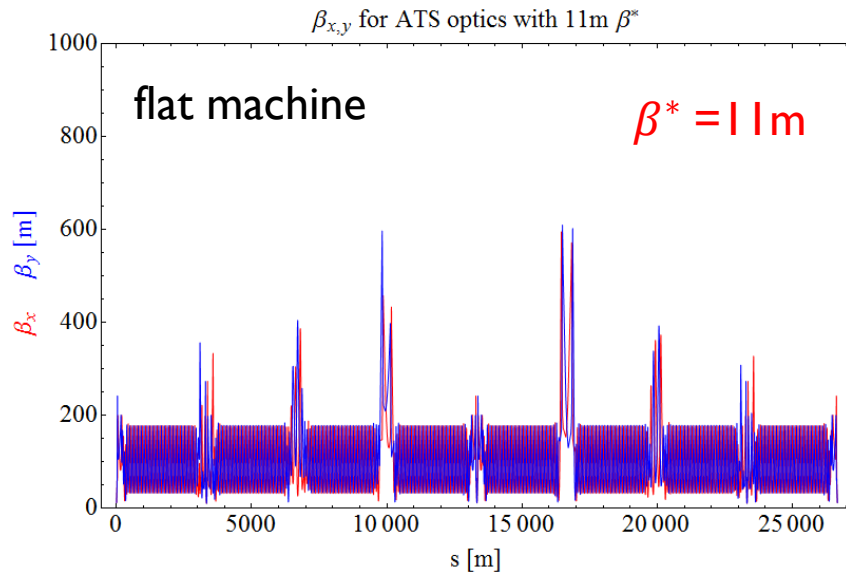
Collisions with round beams @ 7TeV

- Beta Star = 0.1m
- $\frac{1}{2}$ x-angle = 290 microrad (IPI & 5)
- RF voltage = 16MV @ 400MHz
- for the reduced bunch length case with 25ns spacing an additional RF System with 24MV @ 800MHz is necessary
- **ATS version of nominal LHC is used for the analysis**

Taken from: <https://espace.cern.ch/HiLumi/WP2/task4/SitePages/Home.aspx>



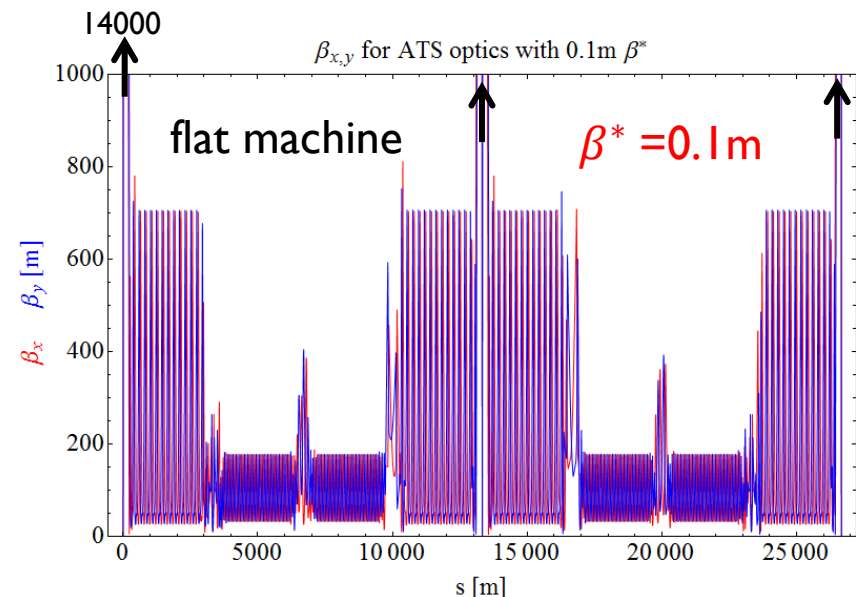
ATS Optics



The effects of the different optics on IBS are studied

1. as a function of β^*
2. for different beam parameters

- ▶ 31 Optics files with β^* values from 11m to 0.1m
- ▶ the squeeze to smaller β^* creates high β -values in the arcs around IPI&5
- ▶ increasing the β -function in arcs starts for $\beta^* \leq 0.4\text{m}$



Injection @ 450GeV

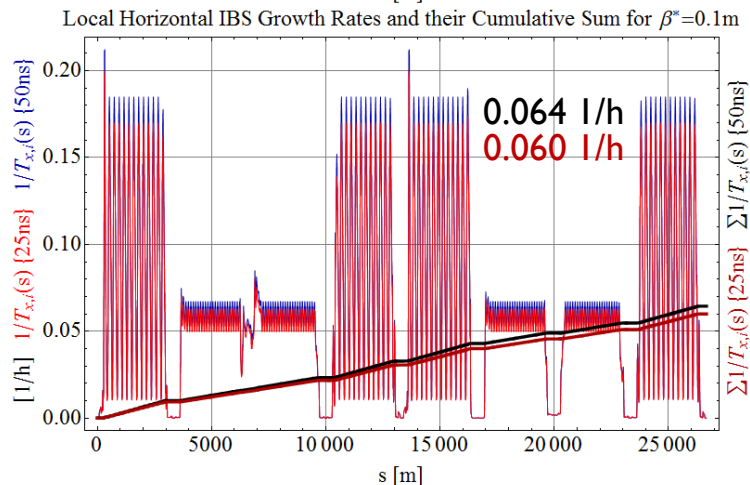
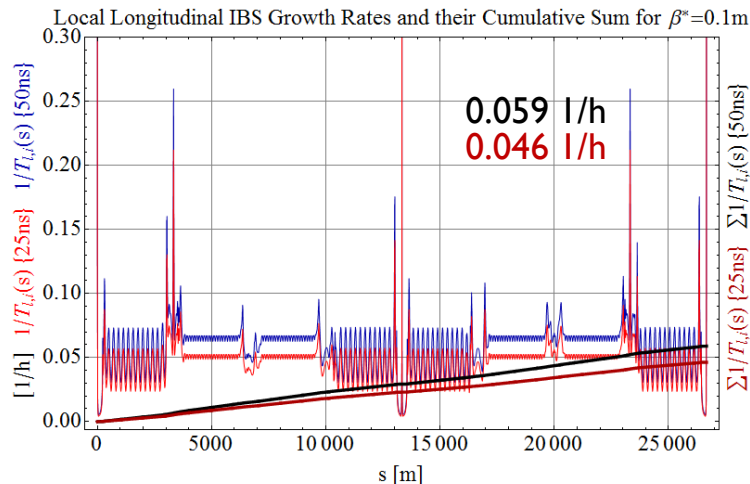
- ▶ IBS growth rates/times at injection energy calculated with MADX
- ▶ at $\beta^* = 11\text{m}$ - ATS optics file I, flat machine
- ▶ all cases are calculated with a longitudinal emittance of 1eVs and with only the main RF system (8MV@400MHz)
- ▶ growth rates increase with increasing intensity and decreasing emittance

	25ns		50ns
Cases	2.2e11, 2.5 μm , 1eVs	2.2e11, 3 μm , 1eVs	3.5e11, 3 μm , 1eVs
1/T _{IBS,l} [1/hour]	0.0964	0.0780	0.124
1/T _{IBS,x} [1/hour]	0.0957	0.0648	0.103
1/T _{IBS,y} [1/hour]	-0.00063839	-0.00043271	-0.00068840

	25ns		50ns
Cases	2.2e11, 2.5 μm , 1eVs	2.2e11, 3 μm , 1eVs	3.5e11, 3 μm , 1eVs
T _{IBS,l} [hour]	10.4	12.8	8.06
T _{IBS,x} [hour]	10.4	15.4	9.70
T _{IBS,y} [hour]	-1566.4	-2311.0	-1452.6

Local contributions of the IBS Growth

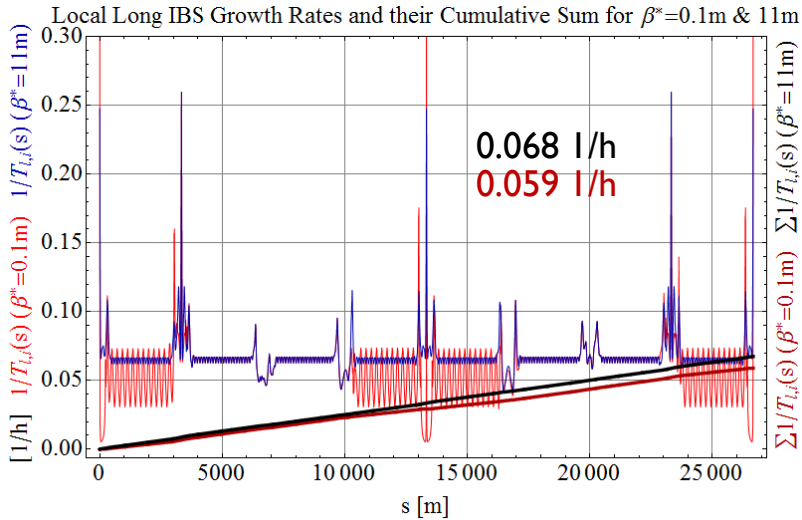
Compare $\beta^* = 0.1\text{m}$ (optics file 31) for 25ns and 50ns nominal cases



- ▶ in the 25ns case (red) the IBS is weaker, due to the relaxed beam parameters
- ▶ longitudinal the cumulative sum increases approx. linear
 - ▶ spikes are quite narrow
 - ▶ the contribution to the total growth rate is similar for all elements
- ▶ the local horizontal growth rates are increased for the high β -regions in the arcs around IPI&5, while the contribution of the straight sections is almost zero, due to the small dispersion
- ▶ the vertical growth is very small and negative (damping)

Local contributions of the IBS Growth

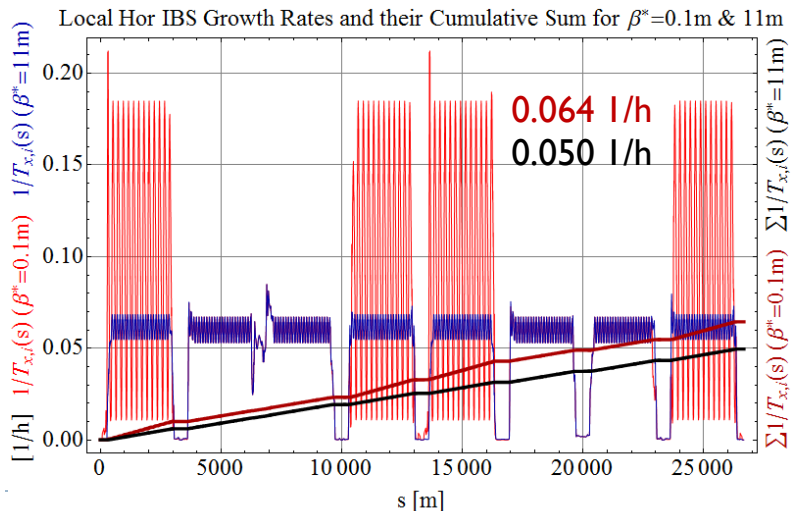
Compare $\beta^* = 11\text{m}$ and $\beta^* = 0.1\text{m}$ (optics file I and 3I) for 50ns case



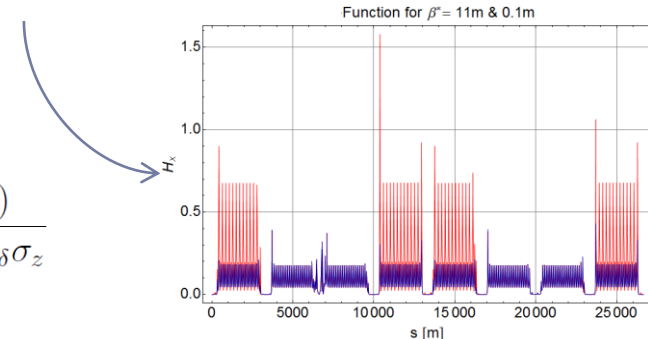
- ▶ longitudinal the squeeze slows down the IBS growth
- ▶ while the growth rates increase in the transverse planes (see next slide), due to the strong contribution of the arcs around IPI&5

$$\begin{pmatrix} \frac{1}{\tau_x} \\ \frac{1}{\tau_l} \\ \frac{1}{\tau_y} \end{pmatrix} = A \begin{pmatrix} \frac{\gamma^2 H_x}{\epsilon_x} \\ \frac{\gamma^2}{\sigma_\delta^2} \\ \frac{\beta_y}{\epsilon_y} \end{pmatrix} \int_0^\infty \left(\frac{\lambda^{1/2}}{(\lambda^3 + a\lambda^2 + b\lambda + c)^{3/2}} \begin{pmatrix} [a_x\lambda + b_x] \\ [a_l\lambda + b_l] \\ [a_y\lambda + b_y] \end{pmatrix} \right) d\lambda$$

$$H_x = \frac{D_x^2}{\beta_x} (1 + \alpha_x^2) + \beta_x D_x'^2 + 2\alpha_x D_x D_x'$$

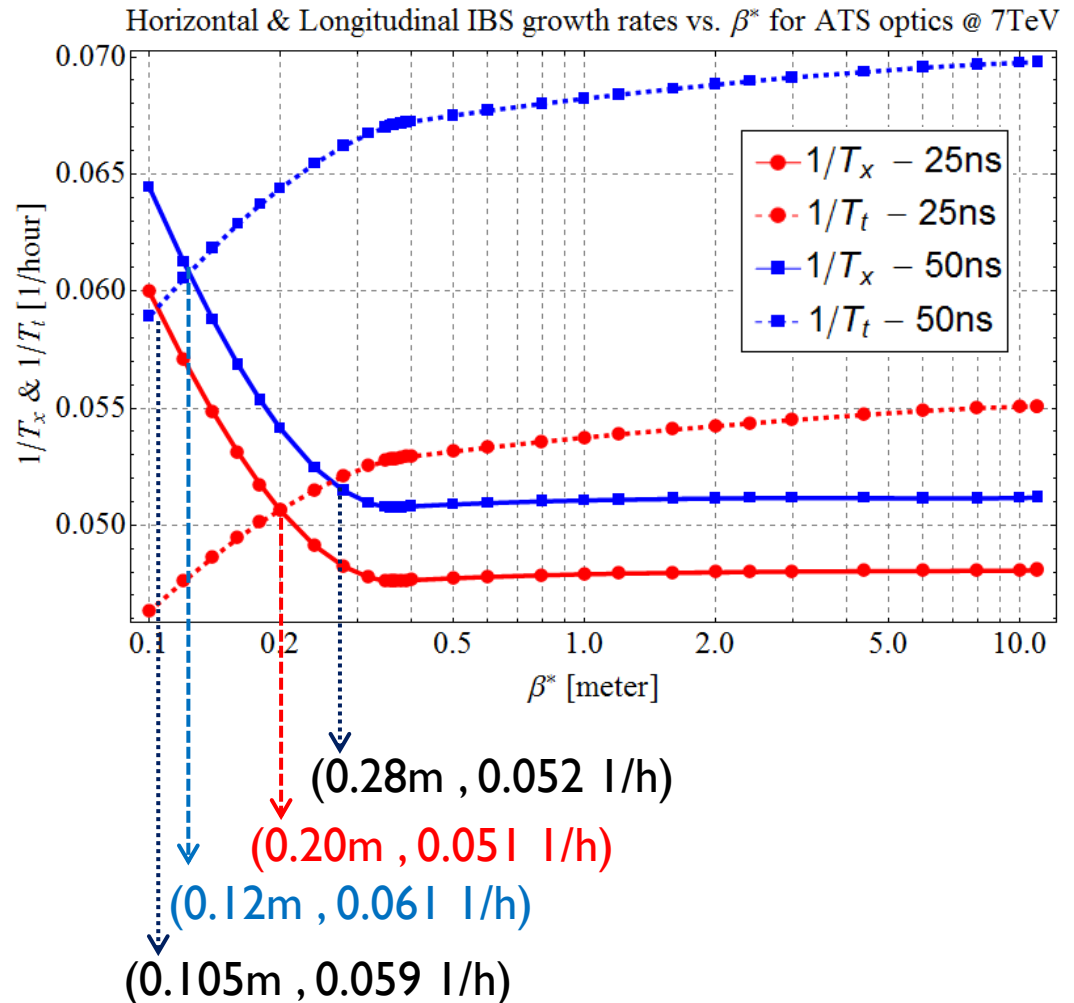


$$A = \frac{r_0^2 v_c N(\log)}{8\pi \beta^3 \gamma^4 \epsilon_x \epsilon_y \sigma_\delta \sigma_z}$$



IBS Growth Rates vs. β^* , 7TeV

- ▶ longitudinal growth rate (dashed line) improves with smaller β^*
- ▶ horizontal growth rate (solid line) increases with β^* smaller $\sim 0.4\text{m}$
- ▶ vertical growth rate shows minimum at around 0.25m (plot in back up slides)



Conclusion

- ▶ Growth rates increase with increasing intensity and decreasing emittance.
 - ▶ Leading to stronger IBS effects for the beam parameters of the 50ns spacing.
 - ▶ IBS growth rates are higher at injection, due to the smaller longitudinal emittance
- ▶ Throughout the squeeze to low β with the ATS optics the longitudinal IBS growth rate improves ($\sim 20\%$), whereas the horizontal growth rate increases ($\sim 20\%$).
 - ▶ Calculations were done for a flat machine.
 - ▶ The increased IBS contribution in the horizontal plane of the high β regions in the arcs around IPI & 5 lead to an increased accumulated IBS growth rate.
 - ▶ In this regions the average longitudinal IBS contribution is reduced

IBS growth times @ 7TeV
for $\beta^* = 0.1\text{m}$ in a flat machine

	25ns	50ns
Cases	2.2e11, 2.5 μm , 7.5cm	3.5e11, 3 μm , 7.5cm
$T_{\text{IBS},1}$ [hour]	21.6	17.0
$T_{\text{IBS},x}$ [hour]	16.7	15.5
$T_{\text{IBS},y}$ [hour]	-6.3624×10^5	-5.9841×10^5

Benchmark Case Proposal

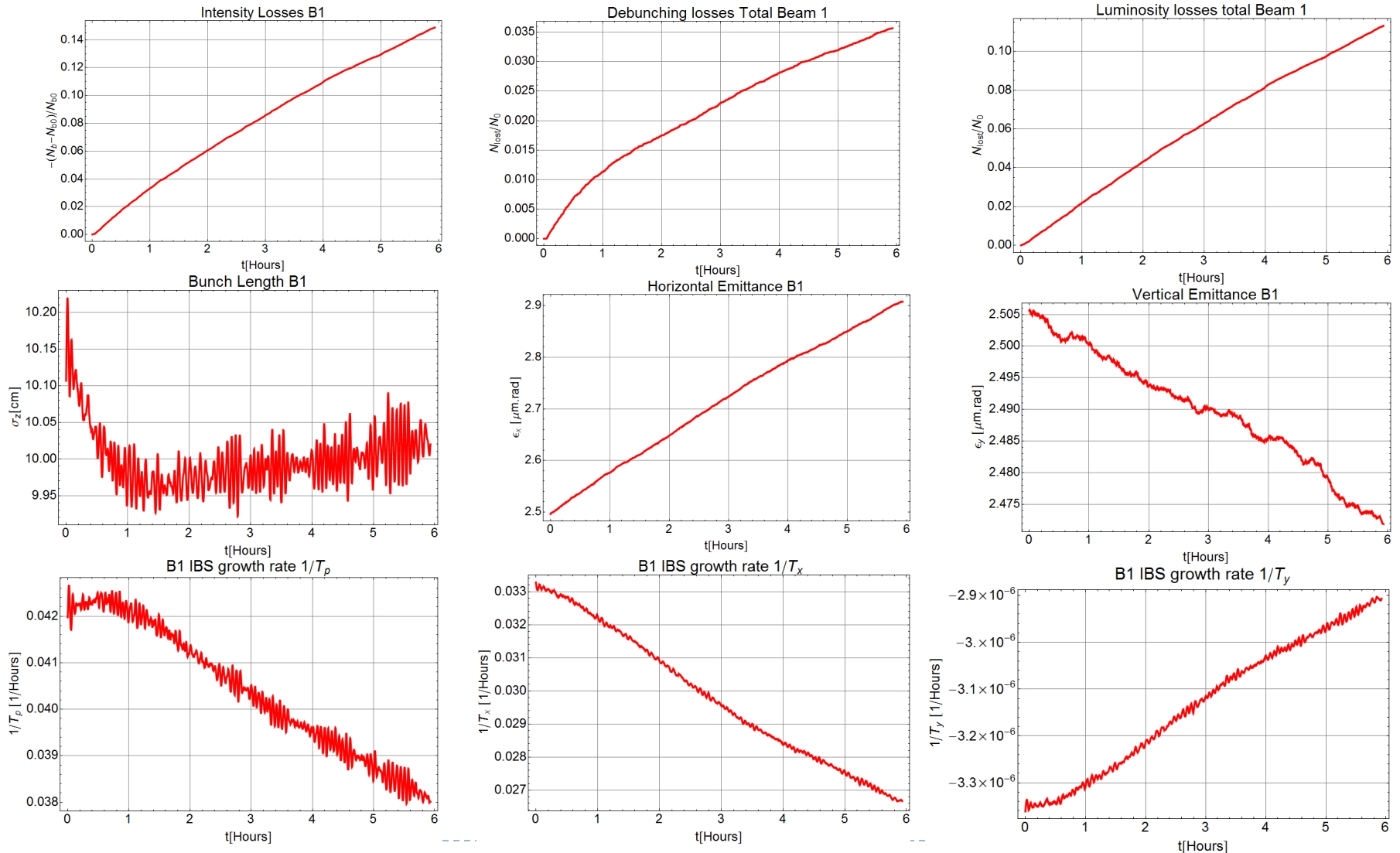
- ▶ Beam parameters from 2012 simulations to compare with reality:

$$\begin{aligned}\varepsilon_N &= 2.5\mu\text{m} \\ N_b &= 1.6 * 10^{11} \text{ ppb} \\ \sigma_t &= 1.35\text{ns} = 10.1\text{cm} \\ \beta^* &= (0.6, 3, 0.6, 3)\text{m} \\ \frac{\theta_c}{2} &= 142 \mu\text{rad}\end{aligned}$$

nominal optics
V6.503

Beam	1.6e11, 2.5μm, 1.35eVs	
Program	CTE	MADX
$T_{\text{IBS},1}$ [hour]	23.8	27.7
$T_{\text{IBS},x}$ [hour]	30.1	29.3
$T_{\text{IBS},y}$ [hour]	-2.98×10^5	2.43×10^3

Beam Evolution of the Benchmark Case



Plans for the future...

- ▶ Simulations with CTE for ATS optics
- ▶ Calculations and Simulations based on the SLHC optics (SLHCV3.1b)
 - ▶ IBS growth rates at injection and in physics
- ▶ Redo the calculations with MADX shown in this presentation with bumps and crossing angles in the machine
 - ▶ CTE does not use this information in the IBS calculations

BACK- UP

Collider Time Evolution (CTE) Program

Processes taken into account:

▶ COLLISIONS

- ▶ user can choose between 2 collision routines:
 - ▶ very slow, integrates interaction probability for every particle by sorting particles in opposing beam in discrete bins. **No assumptions on the shape of the beam distribution.**
 - ▶ fast routine, **assumes Gaussian transverse distribution** and calculates interaction probability from transverse distribution analytically and uses **global reduction factor** (hourglass and crossing angle) for all particles. **No assumptions on longitudinal distribution.**

▶ IBS

- ▶ rise time calculated using a standard method and modulated to account for non-Gaussian longitudinal profiles
- ▶ user can choose between the following methods:
 - ▶ Nagaitsev full lattice
 - ▶ smooth lattice Piwinski
 - ▶ full lattice Piwinski
 - ▶ full lattice modified Piwinski
 - ▶ full lattice Bane (*not good at injection*)
 - ▶ interpolation from tabulated risetimes in external file at given points in emittance-space

▶ BETATRON MOTION

▶ SYNCHROTRON MOTION (particles outside RF bucket are lost)

▶ RADIATION DAMPING and QUANTUM EXCITATION

▶ transverse aperture cut from COLLIMATION

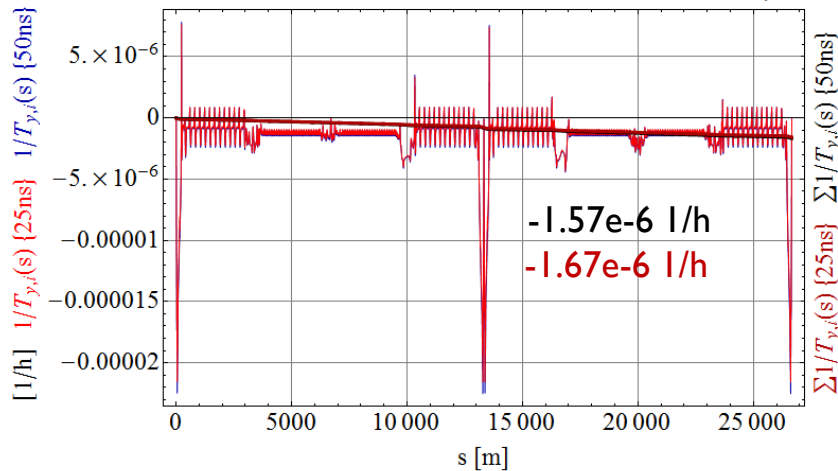
Collider Time Evolution (CTE) Program

- ▶ **Output on a turn-by-turn basis**
 - ▶ IBS rise times
 - ▶ Intensity
 - ▶ Transversal and longitudinal emittances
 - ▶ Luminosity

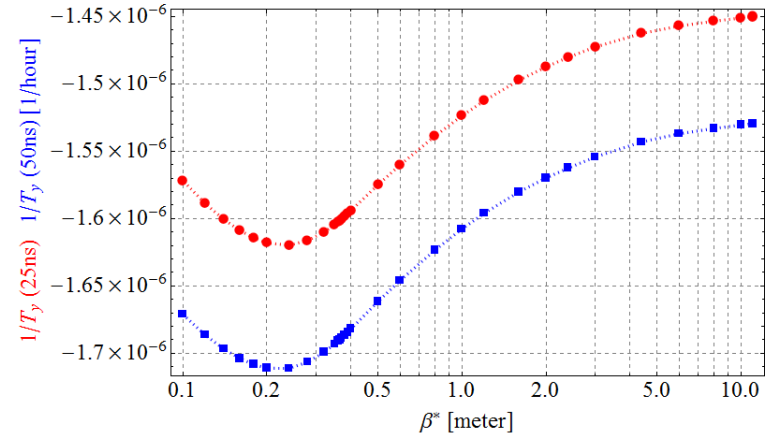
- ▶ **Not Implemented**
 - ▶ Beam-Beam effects
 - ▶ Betatron noise from feedback
 - ▶ emittance blow-up
 - ▶ RF noise
 - ▶ Elastic and inelastic beam gas scattering
 - ▶ particle loss and emittance blow-up

IBS Growth in the Vertical Plane

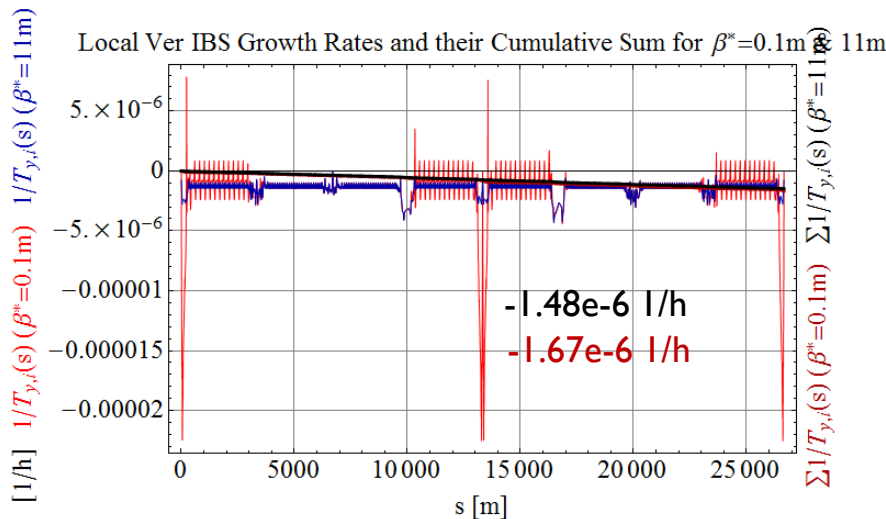
Local Vertical IBS Growth Rates and their Cumulative Sum for $\beta^* = 0.1\text{m}$



Vertical IBS growth rates vs. β^* for ATS optics @ 7TeV



Local Ver IBS Growth Rates and their Cumulative Sum for $\beta^* = 0.1\text{m}$ @ 11m



- ▶ vertical IBS growth rate very small and negative (damping)
- ▶ calculations done for flat machine
- ▶ if x-angle and vertical dispersion is introduced this behaviour may not be realised any more!