## POWER SPECTRA

COMPARISON BETWEEN DIFFERENT TYPES OF LONGITUDINAL BUNCH PROFILES FOR THE LHC

### **Elias Métral**

- Examples of measured bunch spectra
- Comparison of 4 very different longitudinal bunch profiles and corresponding power spectra
- Comparison of several longitudinal bunch profiles close to Gaussian ones (BUT with finite tails), and power spectra
- What is the (simple) distribution fitting best the 2 measurements: Before Ramp and Stable Beams
- Conclusion
- Appendix: some formulae

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#### **EXAMPLES OF MEASURED BUNCH SPECTRA**

#### Measurements on B1 by Themis and Philippe on fill # 2261



**Reminder on the power loss/deposited [W]**  $P_{loss} = M I_b^2 Z_{loss}$ 

$$Z_{loss} = 2 M \sum_{p=1}^{\infty} \text{Re} \left[ Z_l \left( p M \omega_0 \right) \right] \times \text{PowerSpectrum} \left[ p M \omega_0 \right]$$

$$I_b = N_b \ e \ f_0$$

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# **4 THEORETICAL LONGITUDINAL BUNCH PROFILES** Line density $\times \tau_{\rm h}$ $\tau_b = 4 \sigma$ Parabolic amplitude density Gaussian amplitude density Parabolic line density Water - bag bunch 0.5 $\boldsymbol{\tau}$ $au_{b}$ / 2 -0.5-1.5 0.5 1

## **CORRESPONDING POWER SPECTRA (1/2)**



 $\tau_b = 1.2 \text{ ns}$ 



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## COMPARING LONGITUDINAL BUNCH PROFILES CLOSE TO GAUSSIAN BUT WITH FINITE TAILS (1/7)



## COMPARING LONGITUDINAL BUNCH PROFILES CLOSE TO GAUSSIAN BUT WITH FINITE TAILS (2/7)



## COMPARING LONGITUDINAL BUNCH PROFILES CLOSE TO GAUSSIAN BUT WITH FINITE TAILS (3/7)



## COMPARING LONGITUDINAL BUNCH PROFILES CLOSE TO GAUSSIAN BUT WITH FINITE TAILS (4/7)



## COMPARING LONGITUDINAL BUNCH PROFILES CLOSE TO GAUSSIAN BUT WITH FINITE TAILS (5/7)



## COMPARING LONGITUDINAL BUNCH PROFILES CLOSE TO GAUSSIAN BUT WITH FINITE TAILS (6/7)



## COMPARING LONGITUDINAL BUNCH PROFILES CLOSE TO GAUSSIAN BUT WITH FINITE TAILS (7/7)





Maybe not too bad (with the 2<sup>nd</sup> dip hidden for some reason…)



#### CONCLUSION

- I made an error in some previous estimates and thought that the LHC longitudinal profile was close to a water-bag one (as the agreement was so good I did not check everything!...)
  - => See <u>https://indico.cern.ch/getFile.py/access?</u> contribld=65&sessionId=5&resId=0&materialId=slides&confld=150 474
- I checked (or at least tried to...) my computations (still to be checked by others! Thanks in advance => I gave the procedure in the Appendix)
- It seems now that the LHC longitudinal profile is maybe not too far from a Gaussian-like distribution with finite tails (n=3) before the ramp
- However, in stable beams I cannot fit it reasonably with the simple distributions used in these slides => Effect of the longitudinal blow-up to be followed up...

#### **APPENDIX: SOME FORMULAE (1/3)**

#### Plot of the analytical spectra

- Several distributions considered to compute the power spectra => See Laclare, CAS, CERN 87-03, page 268, Eqs. (25) to (28) + a family of distributions close to Gaussian one but with finite tails (similar to what was done in the past for the transverse plane: <u>http://cdsweb.cern.ch/record/733611/files/ab-2004-019.pdf</u>, assuming the same Half-Width at Half-Maximum)
- Amplitude A of the spectrum for a given frequency => Page 267, Eq. (23)
- Normalize the amplitude spectrum by the spectrum at 0 frequency
  => A / A<sub>0</sub>
- The power spectrum (in dB) is obtained by taking 20 Log[10, A /A<sub>0</sub>]

#### **APPENDIX: SOME FORMULAE (2/3)**

(Simple) computation of the power loss for the case of a (sharp) resonance

- Let's assume a longitudinal resonance defined by (f<sub>r</sub>, R<sub>l</sub>, Q) with a high Q
- The power loss can be written  $P_{loss} = (M I_b)^2 \times R_l \times 10^{-10}$ where  $P_{dB}$  ( $f_r$ ) is the power in dB read from a power spectrum (computed or measured) at the frequency  $f_r$
- Note that in the case of a Gaussian bunch, the power loss is written  $P_{loss}^{Gaussian} = (M I_b)^2 \times R_l \times e^{-(2\pi f_r \sigma_\tau)^2}$

$$I_b = N_b \ e \ f_0$$

 $\underline{P_{dB}}\left(f_{r}\right)$ 

#### **APPENDIX: SOME FORMULAE (3/3)**

Why write the power loss as in page 2 (see for instance: Furman, Lee, Zotter, Energy Loss of Bunched Beams in SSC RF Cavities)?

- Because in this case we see clearly that
  - For a broad-band impedance, the sum can be replaced by an integral and the *M* in front disappears => Power loss proportional to *M* (i.e. it is *M* times the single-bunch case)
  - For a narrow band impedance, the sum is only 1 term (see previous page) => Power loss proportional to M<sup>2</sup> (i.e. it is NOT M times the single-bunch case)

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