



 ICE action 8 (XB and AB): Clarify the situation with the stability diagram in the presence of both octupoles and LR beambeam



Stability diagrams

- An oscillation mode is represented by its complex tune shift
- It depends mainly on :
 - The machine impedance
 - The beam intensity
 - The chromaticity
 - The nature of the mode





Stability diagrams

- Representation of the effect of Landau damping on impedance driven mode
 - \rightarrow The limit of stability is higher than Im(ΔQ) = 0
- Depends mainly on :
 - The amplitude detuning
 - The beam distribution (i.e. the beam emittance)







Models :

- Tracking with MAD-X
- Numerical evaluation of the dispersion integral



- Python Solver for Stability Diagrams)
- Full LHC complexity included but :
 - "Large" computing time
 - Numerical noise

al noise 2D dispersion integral, $\frac{-1}{\Delta Q} = \iint \frac{J_x \frac{\partial \Psi}{\partial J_x} dJ_x dJ_y}{Q_0 - Q_x (J_x, J_y)}$



Models : AB approx



$$\Delta_{bb}Q_{x}^{(1)} = \frac{3 |\Delta_{bb}Q_{x}^{(0)}|}{2r^{2}} \frac{J_{x} - 2J_{y}}{\varepsilon}$$

- Δ_{bb}Q_x⁽⁰⁾ is the tune shift for a single IP, AB uses 2.5E-3
- r is the normalized separation, AB uses 9.3
- Total detuning with IP1&5 is twice $\Delta_{bb}Q_{x}^{(1)}$
 - Linear detuning (r >> 1)
 - Constant separation
 - No // separation
 - IP1&5 only, with alternating Xing

MAD-X tracking without // separation MAD-X tracking with // separation AB approx



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Why such a large impact on the stability diagram ?



0.0

-2.5

-2.0



 Linear detuning is over-estimated

-1.5 - 1.0 - 0.5

 $Re(\Delta Q)$

0.0

0.5

 $\times 10^{-3}$



Long-range non-linearity













 Parallel separation does play an important role



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1.5• 175 % over (0 ∇) шestimation of LR component at the end of the squeeze 0.5(in term of "octupole equivalent")







Fig. 3: LHC stability diagrams: a separated stable beam with +200A of the Landau octupoles (green); pacman beam-beam only (no octupoles) at the end of the squeeze (blue); this pacman beam-beam and +500A of the octupoles in addition (black); same as the black line plus e-cloud with total $N_e = (1.3, 1.5, 1.7) \cdot 10^{10}$ (magenta, red, brown). Markers of the corresponding colour show the most unstable modes.





Conclusion



- The linear detuning is over-estimated by AB approx, compared to MAD-X, even without considering the parallel separation
- Long range beam-beam is not an octupole and higher order multipoles have an impact on the stability diagrams
- The parallel separation at the end of the squeeze is on, and it does have an impact on the stability diagram